## Mark schemes





(a)

(a)

13

(i)  $\Delta m = Zm_{\rm p} + (A - Z)m_{\rm n} - M$  (1)

(ii) binding energy per nucleon = 
$$\frac{(\Delta m)c^2}{A}$$
 (1)

2

[7]

(b)	(i)	A in range $54 \rightarrow 64$ (1) stability increases as binding energy per nucleon increases (1)	
		[or binding energy per nucleon is a measure of stability] [or large binding energy per nucleon shows nucleus is difficult to break apart]	
	(ii)	binding energy per nucleon increases from about 7.6 to 8.5 (1) increase of about 0.9 MeV for 235 nucleons (1) bence 210 MeV (≈ 200 MeV) in total (1)	
		5	[7]
	(i)	Eission accurs at A values above the neak / above A of about 56 and fusion accurs a	+
<b>15</b> <sup>(a)</sup>	(1)	A values below the peak / below A of about 56 $\checkmark$	ι
		Fission is the splitting of a nucleus (into two smaller ones) and fusion is the joining of two nuclei $\checkmark$	
		First mark uses the graph so 'fission occurs in very large nuclei' does not gain a mark. (allow other interpretations that use the graph eq gradients)	
		2nd Mark splitting into 2 is not required for fission but if the answer	
		implies something different like the separating of all the nucleons the mark may not be given.	
			2
	(ii)	Energy is released when the binding energy (per nucleon) is increased $\checkmark$ fusion energy is greater as the increase in BE(/A) for fusion > increase in BE(/A) for fission (owtte) $\checkmark$	
		The last point can be given for a reference to the larger gradient at small values of A (fusion region) compared to the gradient at large values of A (fission region)	
			2
(b)	(i)	$\Delta m = (8m_p + 8m_n) - M_{oxygen}$ mark for substituting data into the above equation in any workable consistent units	
		= 8(1.00867+1.00728) - 15.991 ✓	
		(∆ <i>m</i> = 0.1366 u	
		$\Delta m = 0.1366 \times 1.661 \times 10^{-27}$ ) = 2.3 × 10 <sup>-28</sup> (kg) $\checkmark$	
		(range of answers 2.2 - 2.3 × $10^{-28}$ kg)	
		Substitution may take the following form	
		$8(1.673 \times 10^{-27})+8(1.675 \times 10^{-27})-(15.991 \times 1.661 \times 10^{-27})$	
		$= 2.23 \times 10^{-26} \text{ (kg) } \checkmark$	
		Look out for a physics error in which u is not taken as $1.661 \times 10^{-27}$	
		kg	2
	utor	facabaak com/ThaOnlinaDhu	, ciccTi

	(ii)	$E = m \times c^{2} = 2.3 \times 10^{-28} \times (3.00 \times 10^{8})^{2} = 2.07 \times 10^{-11} \text{ J}$ BE = 2.07 × 10 <sup>-11</sup> / 1.6 × 10 <sup>-13</sup> = 130 (MeV) ✓ (129 MeV) Or using using $\Delta m = 0.1366$ u (this must appear in b(i) for this approach) BE = 0.1366 × 931.3 = 130 (MeV) ✓ (127 MeV) <i>CE is allowed but only if the calculation is shown</i> <i>Note answer</i> = b(i) × 5.625 × 10 <sup>29</sup>	. ,		
		answer only is acceptable for one mark. (factor may be 931 or 931.5)		1	
	(iii)	read from the graph the BE/A for ${}^{16}_{8}$ O and multiply by the number of nucleon $\checkmark$	s (or ′	16)	
		Or show the calculation BE = 8(Mev) × 16(nucleons) = 130 (MeV) $\checkmark$ (128 MeV) $\checkmark$ There must be a reference to ${}^{16}_{8}$ o position on the graph. with the calculation allow BE = 8.1(Mev) × 16(nucleons) = 130 (MeV)			
		A calculation may lead to an answer in joule		1	[8]
(a)	nucl	eon number 4	B1		
	proto	on number 2	B1	(2)	
(b)	(i)	mass of products is less than mass of reactants / binding energy per nucleor increases / mass defect increases / 'loss' of mass	ר B1		
		change in mass converted to energy	B1	(2)	
	(ii)	change in mass = $4.8 \times 10^{-29} \text{ kg}$	C1		
		$E = mc^2$	C1		
		$4.3 \times 10^{-12} \text{ J} (4.30 \times 10^{-12} \text{ J})$			
		(if truncated sig. figs used only 2nd mark available)	A1	(3)	[7]

2

1

(a) (using mass defect = Δm = Z m<sub>p</sub> + N m<sub>n</sub> - M<sub>Co</sub>) Δm = 27 × 1.00728 + 32 × 1.00867 - 58.93320 (u) ✓ Δm = 0.5408 (u) ✓ Binding Energy = 0.5408 × 931.5 = 503.8 (MeV) ✓ (CE this mark stands alone for the correct energy conversion even if more circular routes are followed.

Look at use of first equation and if electrons are used or mass of proton and neutron confused score = 0.

If subtraction is the wrong way round lose 1 mark.

Data may come from rest mass eg  $m_n$  =939.551 MeV or 1.675 × 10<sup>-27</sup> kg or 1.00867 u.

So if kg route used  $\Delta m = 8.83 \times 10^{-28}$  kg BE = 7.95 × 10<sup>-28</sup> J and 497 Mev.

Conversion mark (2nd) may come from a wrong value worked through. 0.47(5)

(b)  $(2.52 - 1.76) \times 10^{-13} = 7.6 \times 10^{-14} \text{ J} \checkmark$ 

 $7.6 \times 10^{-14}$  /  $1.60 \times 10^{-13}$  = 0.47 or 0.48 MeV √(0.475 MeV) Correct answer scores both marks.

(c) 6 (specific wavelengths)

+ + +

(d) (longest wavelength = lowest frequency = smallest energy)
(2.29 × 10<sup>-13</sup> - 2.06 × 10<sup>-13</sup>) = 2.3 × 10<sup>-14</sup> (J) ✓
λ (= h c / E) = 6.63 × 10<sup>-34</sup> × 3.00 × 10<sup>8</sup> / 2.3 × 10<sup>-14</sup> ✓
λ = 8.6 - 8.7 × 10<sup>-12</sup> (m) ✓ (8.6478 × 10<sup>-12</sup> m)
Allow a CE in the second mark only if the energy corresponds to an energy gap including those to the ground state.
The allowed energy gaps for CE are:
2.29, 2.06, 1.76, 0.53, 0.30 all × 10<sup>-13</sup>
Note substitution rather than calculation gains mark.
The final mark must be as shown here and not from a CE above.

3

[9]

1

3

2

 (a) the amount of energy required to separate a nucleus √ into its separate neutrons and protons / nucleons √
 (or energy released on formation of a nucleus √ from its separate neutrons and protons / constituents √)

1<sup>st</sup> mark is for correct energy flow direction
2<sup>nd</sup> mark is for binding or separating nucleons (nucleus is in the question but a reference to an atom will lose the mark) ignore discussion of SNF etc both marks are independent

(b) (i)  $2_0^1 n \text{ or } {}_0^1 n + {}_0^1 n \checkmark$ 

must see subscript and superscripts

(ii) binding energy of U
 = 235 × 7.59 √ ( = 1784 (MeV))

binding energy of Tc and In

= 112 × 8.36 + 122 × 8.51 √

( = 1975 (MeV))

energy released ( = 1975 - 1784) = 191 (MeV) √ (allow 190 MeV)

 $1^{st}$  mark is for 235 × 7.59 seen anywhere

 $2^{nd}$  mark for  $112 \times 8.36 + 122 \times 8.51$  or 1975 is only given if there are no other terms or conversions added to the equation (ignore which way round the subtraction is positioned) correct final answer can score 3 marks

```
(iii) energy released
```

```
= 191 \times 1.60 \times 10^{-13} \checkmark

(= 3.06 \times 10^{-11} J)

loss of mass (= E/c^2)

= 2.91 \times 10^{-11} / (3.00 \times 10^8)^2)

= 3.4 \times 10^{-28} (kg) \checkmark

or

= 191 / 931.5 u \checkmark (= 0.205 u)

= 0.205 \times 1.66 \times 10^{-27} (kg)

= 3.4 \times 10^{-28} (kg) \checkmark

allow CE from (ii)

working must be shown for a CE otherwise full marks can be given

for correct answer only

note for CE

answer = (ii) \times 1.78 \times 10^{-30}

(2.01 \times 10^{-27} is a common answer)
```

(c) (i) line or band from origin, starting at 45° up to Z approximately = 20 reading  $Z = 80, N = 110 \rightarrow 130 \checkmark$ 

initial gradient should be about 1 (ie Z = 20;  $N = 15 \rightarrow 25$ ) and overall must show some concave curvature. (Ignore slight waviness in the line) if band is shown take middle as the line if line stops at N > 70 extrapolate line to N = 80 for marking

(ii) fission fragments are (likely) to be above / to the left of the line of stability  $\sqrt{}$  fission fragments are (likely) to have a larger N/Z ratio than stable nuclei or

fission fragments are neutron rich owtte  $\checkmark$  and become neutron or  $\beta^-$  emitters  $\checkmark$ 

ignore any reference to  $\alpha$  emission a candidate must make a choice for the first two marks stating that there are more neutrons than protons is not enough for a mark  $1^{st}$  mark reference to graph  $2^{nd}$  mark – high N / Z ratio or neutron rich  $3^{rd}$  mark beta <u>minus</u> note not just beta

(a) (i) heat water to 100 °C, energy (= 190 × 4200 × 79) = 63 (MJ) (1) vapourise water, energy (=190 × 2.3 × 10<sup>6</sup>) = 440(MJ) (1) (437MJ)

energy transferred (per sec) = (437 + 63) MJ (1) (= 500 MJ)

(ii) mass of rocks (=  $4.0 \times 10^6 \times 3200$ )

=  $1.3 \times 10^{10}$ (kg) (1) (1.28 × 10<sup>10</sup>)

temperature fall of  $\Delta T$  in one day, energy removed (= 1.28 ×10<sup>10</sup> × 850 ×  $\Delta T$ ) = 1.1 × 10<sup>13</sup>  $\Delta T$  (1)

 $(1.09 \times 10^{13} \text{ AT})$ (allow C.E. for value of mass of rocks)

energy transfer in one day (=  $500 \times 10^6 \times 3600 \times 24$ ) =  $4.3 \times 10^{13}$  (J) (1)

in one day  $\Delta T \left( = \frac{4.3 \times 10^{13}}{1.1 \times 10^{13}} \right) = 3.9(1)$  K (1)

7

19

1

[12]

## theonlinephysicstutor.com

(b) number of nuclei in 1 kg of <sup>238</sup> U = 
$$\left(\frac{6.02 \times 10^{23}}{0.238}\right) = 2.5(3) \times 10^{24}$$
 (1)

activity of lkg of <sup>238</sup>U =  $\frac{1n2}{T_{1/2}} \times 2.53 \times 10^{24}$  (1)

$$\left(=\frac{1n2}{4.5\times10^9\times3.1\times10^7}\times2.53\times10^{24}\right)=1.2(6)\times10^7\,(s^{-1})$$
 (1)

energy released per sec per kg of 238 U

= 
$$1.2(6) \times 10^7 \times 4.2 \times 1.6 \times 10^{-13}(J)$$
 (1)  
(8.47 × 10<sup>-6</sup>(J))

mass of <sup>238</sup>Uneeded =  $\frac{500 \times 10^6}{8.47 \times 10^{-6}}$  = 5.9(0) × 10<sup>13</sup>kg (1)

1

2

[12]
------

20	
----	--

(a)

(i) 1/12 the mass of an (atom) of <sup>12</sup><sub>6</sub> C / carbon−12 / C12 ✓
 a reference to a nucleus loses the mark

(ii) separated nucleons have a greater mass ✓ (than when inside a nucleus)
 an answer starting with 'its' implies the nucleus

because of the (binding) energy <u>added</u> to <u>separate</u> the nucleons or energy is <u>released</u> when a nucleus is <u>formed</u> (owtte) ✓ *marks are independent* 

direction of energy flow or work done must be explicit

(b) nuclei need to be <u>close together</u> (owtte) for the Strong Nuclear Force to be involved or for fusion to take place ✓

e.g. first mark - within the range of the SNF

but the electrostatic / electromagnetic force is repulsive (and tries to prevent this) 🗸

(if the temperature is high then) the nuclei have (high) kinetic energy / speed (to overcome the repulsion)  $\checkmark$ 

3<sup>rd</sup> mark is for a simple link between temperature and speed / KE

3

(c) (i) 15 🗸

give the middle mark easily for any e or  $\beta$  with a + in any position

 $e^+ \checkmark (or \beta^+, {}^0_1 \beta, {}^0_1 e)$ 

12 🗸

@TOPhysicsTutor

facebook.com/TheOnlinePhysicsTutor Page 9 of 15

		theorimephysic	Stutor.C
	(ii)	$\Delta mass = 4 \times 1.00728 - 4.00150 - (2 \times 9.11 \times 10^{-31} / 1.661 \times 10^{-27})$	
		Δmass = {4 × 1.00728 − 4.00150 − 2 × 0.00055}(u) ✓	
		(4×1.00728=4.02912)	
		1 <sup>st</sup> mark – correct subtractions in any consistent unit. use of $m_p = 1.67 \times 10^{-27}$ kg will gain this mark but will not gain the 2 <sup>nd</sup> as it will not produce an accurate enough result	
		∆mass = 0.02652(u) ✓	
		2 <sup>nd</sup> mark - for calculated value	
		0.02652u	
		$4.405 \times 10^{-29} \text{ kg}$	
		$3.364 \times 10^{-12} J$	
		Δbinding energy (= 0.02652 × 931.5) {allow 931.3}	
		∆binding energy = 24.7 MeV ✓	
		3 <sup>rd</sup> mark – conversion to Mev	
		conversion mark stands alone	
		award 3 marks for answer provided some working shown - no working gets 2 marks	
		(2sf expected)	
			3
			[12]
(a)	Draw	vs appropriate triangle on graph or other mark on graph at ~ 118	
		B1	
	Cha	nge of approx 1 Me V per nucleon is multiplied by 235	
		B1	
	Mult	tiplies by $1.6 \times 10^{-13}$	
		B1	
		2.	
	Quo	tes their answer of approx 3.8 $\times$ 10 <sup>-11</sup> to more than 2 sf	
		B1	
			4

theonlinephysicstutor.com

(b)	(2 × 2.0135) – 4.0026 seen or 0.0244 (u)		
		C1	
	Multiplies u by 1.7 × $10^{-27}$		
		C1	
	$E = mc^2$ seen or multiplies by $(3 \times 10^8)^2$		
		C1	
	3.67 × 10 <sup>−12</sup> J		
		A1	
			4
(c)	Multiplies $3.8 \times 10^{-11}$ or their (b) by $6 \times 10^{23}$		
		M1	
	attempts to convert to energy per kg by multiplying by 1000 / 4 or 1000 / 235		
		M1	
	Compares 5.5 × $10^{14}$ (J) (Hydrogen) with 9.6 × $10^{13}$ (J) (Uranium) in solvay eg by stating that the fusion reaction gives more energy (per kg) the fission or very similar values – must be consequent on some correct	ne an t analysis	
		A1	2
(d)	Availability of fuel easier for fusion		3
		B1	
	Doesn't produce radioactive fission products / no waste management problem		
		B1	
			2

**22** (a)

(i)

(Mass change in u=)  $1.71 \times 10^{-3}$  (u) or (mass Be-7) – (mass He-3) – (mass He-4) seen with numbers

C1 2.84 × 10<sup>-30</sup> (kg) or Converts their mass to kg Alternative 2nd mark: Allow conversion of  $1.71 \times 10^{-3}$  (u) to MeV by multiplying by 931 (=1.59 (MeV)) seen C1 Substitution in  $E = mc^2$ condone their mass difference in this sub but must have correct value for  $c^2 (3 \times 10^8)^2$  or  $9 \times 10^{16}$ Alternative 3rd mark: Allow their MeV converted to joules (x  $1.6 \times 10^{-13}$ ) seen C1  $2.55 \times 10^{-13}$  (J) to  $2.6 \times 10^{-13}$  (J) Alternative 4th mark: Allow  $2.5 \times 10^{-13}$  (J) for this method A1 4 Use of  $E=hc/\lambda$  ecf (ii) C1 Correct substitution in rearranged equation with  $\lambda$  subject **ecf** C1  $7.65 \times 10^{-13}$  (m) to  $7.8 \times 10^{-13}$  (m) ecf A1 3 Use of E<sub>p</sub> formula: (b) (i) C1 Correct charges for the nuclei and correct powers of 10 C1 2.6(3) × 10<sup>-13</sup> J A1 3

				theonli	nephysi	cstutor.com
		(11)	Uses $KE = 3 / 2 KI$ : or halves $KE_T$ , $KE = 1.3 \times 10^{-13}$ (J) seen ecf			
					C1	
			Correct substitution of data <b>and</b> makes T subject <b>ecf</b> Or uses $KE_T$ value <b>and</b> divides T by 2			
					C1	
			6.35 × 10 <sup>9</sup> (K) or 6.4 × 10 <sup>9</sup> (K) or 6.28 × 10 <sup>9</sup> (K) or 6.3 × 10 <sup>9</sup> (K) <b>ecf</b>			
					A1	3
	(c)	(i)	Deuteron / deuterium / hydrogen-2			
					B1	
			Triton / tritium / hydrogen-3			
					B1	2
		(ii)	Electrical heating / electrical discharge / inducing a current in plasma / use of e-m radiation / using radio waves (causing charged particles to resonate)			
					B1	
						1 [16]
23	(a)	(i)	Attempt to use KE = $3/2 kT$ expect $0.75 = 3/2 \times 1.38 \times 10^{-23} T$			
				C1		
			Or correct conversion to J 0.75 × 1.6 × $10^{-19}$			
			Correct equations $0.75 \times 1.6 \times 10^{-19} = 3/2 \ 1.38 \times 10^{-23} \ T$			
				C1		
			5800 K			
				A1	3	

	(ii)	Attempt to use energy = $qQ/4\pi\varepsilon_o r$		
			C1	
		arrives at 1.9(2) ×10 <sup>-9</sup> or uses (2 × 0.75) or twice candidate's energy from (i)		
			C1	
		9.6 × 10 <sup>−10</sup> m		
			A1	3
	(iii)	For fusion nuclei have to touch or separation has to be nuclear diameter		5
		energy has to be sufficient to overcome the nuclear repulsion (between protons)		
			B1	
		Close enough for nuclear strong force to act		
			B1	
		answer to 4 a (ii) is much greater that $10^{-15}$ m		
			B1	
		or is greater that atomic radius		
		or is greater than the range of the strong force		3
(b)	(i)	Use of <i>pV=NkT</i>		5
	( )		C1	
		(Allow incorrect powers of 10 or rearrangement to make <i>N</i> subject)		
		$1 \times 10^{16} \times 1 = N \times 1.38 \times 10^{-23} \times 1.5 \times 10^{6}$		
			C1	
		4.8 (3)× 10 <sup>32</sup>		
			A1	2
				3

	(ii)	1.67 × 10 <sup>-27</sup> or 1.7 × 10 <sup>-27</sup> used		
			C1	
		$8.0 - 8.2 \times 10^5$ (kg m <sup>-3</sup> ) Allow ecf for <i>N</i> from (b)(i)		
			A1	
$(\mathbf{c})$	(i)	Number of protons – moles of proton/mass of protons / Mass		2
(0)	(1)	per second × Avogadro constant used		
			B1	
		Or		
		No of protons = mass per second/proton mass		
		(allow if numerical equation seen with a subject)		
		4.18 or 4.19 or 4.21 × $10^{38}$ correct to at least 2 sf from correct working		
			B1	2
	(ii)	Attempt to use $E = mc^2$ with any mass and substitution for $c$		2
			C1	
		Energy radiated = $5 \times 10^9 \times c^2$ energy radiated $4.5 \times 10^{26}$ J		
			A1	
		Number of helium nuclei formed = $1.05 \times 10^{38}$ (allow 1 × 10 <sup>39</sup> )		
			B1	
		Approximate BE per nucleon from article = $4.28(4.5) \times 10^{-12} \text{ J}$		
			B1	
		(Which is consistent)		4
				4

[20]