

## Mark schemes

**1**

- (a)  $c$  is the same, regardless of the speed of the light source or the observer **(1)**

1

- (b) distance between detectors in rest frame of particles  
 $(= 25 \times (1 - 0.98^2)^{1/2}) = 5.0 \text{ m}$  **(1)**

time taken in rest frame of particles  $\left( = \frac{\text{distance}}{\text{speed}} = \frac{5.0}{0.98c} \right) = 1.7 \times 10^{-8} \text{ s}$  **(1)**

time taken to decrease by  $\frac{1}{4} = 2$  half lives **(1)**

half life  $(= 1.7 \times 10^{-8}/2) = 8.5 \times 10^{-9} \text{ s}$  **(1)**

**[alternatively]**

time taken in rest frame of detectors  $\left( = \frac{\text{distance}}{\text{speed}} = \frac{25.0}{0.98c} \right) = 8.5 \times 10^{-8} \text{ s}$   
 time taken in rest frame of particles  
 $(= 8.5 \times 10^{-8} \times (1 - 0.98^2)^{1/2}) = 1.7 \times 10^{-8} \text{ s}]$

4

**[5]****2**

- (a) (A frame of reference ) that has a constant velocity ✓  
*Accept no acceleration*

1

- (b) (i) Distance = 4.3  $c$  light years ( or  $4.1 \times 10^{16} \text{ m}$ )  
*Correct answer only gets the mark*

Speed  $(= \frac{4.3 c}{5.0}) = 2.6 \times 10^8 \text{ m s}^{-1}$  (or 0.86  $c$ )

*Accept 2.58*

1

(ii)  $t = \left( \frac{t_0}{1 - v^2/c^2} \right)^{1/2}$  where  $t = 5.0$  years (or  $1.58 \times 10^8$  s)

and  $v = 0.86 c$  (or  $2.58 \times 10^8 \text{ m s}^{-1}$ )

*CF from bi to bii provided answer to bi < c*

1<sup>st</sup> mark for correct substitution of either  $t$  or  $v$  into the above eqn ✓

$t_0 = 5.0 \times (1 - (0.86c)^2 / c^2)^{1/2} \checkmark = 2.6$  years ✓

*Accept t or v in alternative units*

*Accept 1.58 (or 1.6) × 10<sup>8</sup> s in place of 5.0 yr in 3<sup>rd</sup> mark point*

**Alt scheme**

$l = l_0 (1 - v^2 / c^2)^{1/2}$  where  $t = 5.0$  years (or  $1.58 \times 10^8$  s) and

$v = 0.86 c$  (or  $2.58 \times 10^8 \text{ m s}^{-1}$ )

*Accept 2.5 to 2.6 to any number of sfs*

1<sup>st</sup> mark for correct substitution of either  $t$  or  $v$  into the above eqn ✓

$(l_0 = 4.3 \times 365 \times 24 \times 3600 \times 3.0 \times 10^8 = 4.07 \times 10^{16} \text{ m})$

$l = 4.07 \times 10^{16} (1 - (0.86c)^2 / c^2)^{1/2}$  or  $2.08 \times 10^{16} \text{ m} \checkmark$

$t_0 = \frac{l}{v} (= \frac{2.08 \times 10^{16} \text{ m}}{2.6 \times 10^8 \text{ m/s}} = 8.05 \times 10^7 \text{ s}) = 2.6$  years ✓

*Alternative for last 2 marks in Alt scheme ( $l_0 = 4.3 \text{ l yr}$ )*

$l = 4.3 (1 - (0.86c)^2 / c^2)^{1/2} = 2.2 \text{ l yr} \checkmark$

$t_0 = \frac{l}{v} (= \frac{2.2}{0.86}) = 2.6$  years ✓

3

[5]

3

(a)  $10m_0 = m_0 \left( 1 - \frac{v^2}{c^2} \right)^{-\frac{1}{2}} \quad (1)$

gives  $\frac{v^2}{c^2} = 1 - 0.01 = 0.99 \quad (1)$

$v (= 0.995c) = 2.98(5) \times 10^8 \text{ m s}^{-1} \quad (1)$

3

(b)  $m = m_0 \left( 1 - \frac{v^2}{c^2} \right)^{-\frac{1}{2}}$  **(1)**

$m \rightarrow$  infinity as  $v \rightarrow c$  **(1)**

[or  $m$  increases as  $v$  increases]

$E_k (= mc^2 - m_0c^2) \rightarrow$  infinity as  $v \rightarrow c$  **(1)**

$v = c$  would require infinite  $E_k$  (or mass) which is (physically)

impossible **(1)**

Max 3

[6]

4

- (a) (i) two beams (or rays) reach the observer **(1)**  
interference takes place between the two beams **(1)**  
bright fringe formed if/where (optical) path difference =  
whole number of wavelengths  
(or two beams in phase)  
[or dark fringe formed if/where (optical) path difference =  
whole number + 0.5 wavelengths]  
(or two beams out of phase by  $180^\circ$  /  $\pi/2$  /  $1/2$  cycle) **(1)**
- (ii) rotation by  $90^\circ$  realigns beams relative to direction of Earth's  
motion **(1)**  
no shift means no change in optical path difference between  
the two beams **(1)**  
 $\therefore$  time taken by light to travel to each mirror unchanged  
by rotation **(1)**  
distance to mirrors is unchanged by rotation **(1)**  
 $\therefore$  no shift means that the speed of light is unaffected  
[or disproves other theory] **(1)**

max 5

- (b) the speed of light does not depend on the motion of the  
light source **(1)** or that of the observer **(1)**

2

[7]

5

(a) (i) Distance travelled in muons' frame of reference  
 $= 10700(1-0.996^2)^{1/2} = 956 \text{ m} \checkmark$   
 Time taken in muons' frame of reference =  $3.2 \mu\text{s} \checkmark$   
 This is 2 half-lives so number reaching Earth = 250  $\checkmark$

**OR**

Time in Earth frame of reference  
 $= 10700 / (0.996 \times 3 \times 10^8) = 3.581 \times 10^{-5} \text{ s} \checkmark$   
 Time taken in muons' frame of reference =  $3.2 \mu\text{s} \checkmark$   
 This is 2 half-lives so number reaching Earth = 250  $\checkmark$

**OR**

Half-life in Earth frame of reference  
 $= 1.6 \times 10^{-6} / (1-0.996^2)^{1/2} = 17.9 \times 10^{-6} \text{ s} \checkmark$   
 Time taken =  $35.8 \times 10^{-6} \text{ s} \checkmark$   
 This is 2 half lives so number reaching Earth = 250  $\checkmark$

**OR**

Distance travelled in muons' frame of reference  
 $= 10700(1-0.996^2)^{1/2} = 956 \text{ m} \checkmark$   
 Distance the muon travels in one half-life in muons reference frame  
 $= 0.996 \times 3 \times 10^8 \times 1.6 \times 10^{-6} = 478 \text{ m} \checkmark$   
 Therefore 2 half-lives elapse to travel 956 m so number = 250  $\checkmark$

**OR**

Decay constant in muon frame of reference  
 Or decay constant in the Earth frame of reference  $\checkmark$

Uses the corresponding elapsed time and decay constant in

$$N = N_0 e^{-\lambda t} \checkmark$$

Arrives at 250  $\checkmark$

*All steps in the working must be seen*

*Award marks according to which route they appear to be taking*

*The number left must be deduced from the correct time that has elapsed in the frame of reference they are using*

3

(ii)

	✓ if correct
For an observer in a laboratory on Earth the distance travelled by a muon is greater than the distance travelled by the muon in its frame of reference	✓
For an observer in a laboratory on Earth time passes more slowly than for a muon in its frame of reference	
For an observer in a laboratory on Earth, the probability of a muon decaying each second is lower than it is for a muon in its frame of reference	

1

- (b) (i) Total energy =  $9.11 \times 10^{-31} \times (3 \times 10^8)^2 / (1-0.98^2)^{1/2}$  ✓  
 $4.12 \times 10^{-13}$  J seen to 2 or more sf ✓

*Show that so working must be seen*

2

- (ii) Change =  $7.5 \times 10^{-14}$  J  
 $V = 469$  (470) kV allow ecf using their answer to (i) ✓  
*ecf is their ((i)  $-3.37 \times 10^{-13}$ ) /  $1.6 \times 10^{-19}$*   
*Using  $4 \times 10^{-13}$  gives 394 (390) kV*  
*Using  $3.9 \times 10^{-13}$  gives 331(330) kV*  
*Do not allow 1 sf answer*

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[7]

6

- (a) (i)  $l = vt = 1.00 \times 10^8 \times 15 \times 10^{-9} = 1.50\text{m}$  (1)

(ii) 
$$l = l_0 \sqrt{1 - \frac{v^2}{c^2}}$$

$$1.50 = l_0 \sqrt{1 - \frac{(1.00 \times 10^8)^2}{(3.00 \times 10^8)^2}} \quad (1)$$

$$l_0 \left( = \frac{1.50}{0.943} \right) = 1.59 \text{ m} \quad (1)$$

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$$(b) \quad (i) \quad m = \frac{m_0}{\sqrt{1 - \frac{v^2}{c^2}}} \quad (1) \quad \text{or} \quad \left[ \frac{m_0}{\sqrt{1 - \frac{(1.00 \times 10^8)^2}{(3.00 \times 10^8)^2}}} \right]$$

$$m \left( \text{or} \frac{m_0}{\sqrt{1 - \frac{(1.00 \times 10^8)^2}{(3.00 \times 10^8)^2}}} \right) = 1.06m_0$$

[or =  $1.06 \times 1.67 \times 10^{-27}$  or  $1.77 \times 10^{-27}$  kg] (1)

kinetic energy =  $(m - m_0)c^2$  (1)

[or =  $0.06m_0c^2$  or  $0.06 \times 1.67 \times 10^{-27} \times (3 \times 10^8)^2$ ]

=  $9.1 \times 10^{-12}$  (J) (1)

(ii) total k.e. =  $(10^7 \times 9.1 \times 10^{-12}) = 9.1 \times 10^{-5}$  (J) (1)

k.e. per second  $\left( = \frac{9.1 \times 10^{-5}}{1.5 \times 10^{-9}} \right) = 6080W$

max 5

[8]

7

(a) speed of light in free space independent of motion of source and / or the observer ✓  
and of motion of observer

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(b) laws of physics have the same form in all inertial frames  
laws of physics unchanged from one inertial frame to another ✓

1

(c) time taken  $\left( = \frac{\text{distance}}{\text{speed}} = \frac{34 \text{ m}}{0.95 \times 3.0 \times 10^8 \text{ m s}^{-1}} \right) = 1.2 \times 10^{-7} \text{ s} \checkmark$

1

(d)  $t = \frac{18 \text{ ns}}{(1 - 0.95^2 c^2 / c^2)^{1/2}} \checkmark$   
*Allow substitution for this mark*

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time taken for  $\pi$  meson to pass from one detector to the other = 58 ns ✓

1

2 half-lives (approximately) in the detectors' frame of reference. ✓

1

two half-lives corresponds to a reduction to 25 % so 75% of the  $\pi$  mesons passing the first detector do not reach the second detector. ✓

OR

Appreciation that in the lab frame of reference the time is about 6 half-lives had passed ✓

1

In 6 half-lives 1 / 64 left so about 90% should have decayed ✓

Clear conclusion made

Either Using special relativity gives agreement with experiment  
or Failure to use relativity gives too many decaying (WTTE)

1

[8]

8

(a) (i) the same or constant **(1)**  
regardless of the speed of the observer or source **(1)**

(ii) physical laws have the same form in all frames **(1)**

(3)

(b) (i)  $T_1$  or beams of mesons =  $8.6 \text{ ns} \times \left(1 - \frac{v^2}{c^2}\right)^{-\frac{1}{2}}$  **(1)**

=  $8.6 \times (1 - 0.95^2)^{-\frac{1}{2}} = 27.5 \text{ ns}$  **(1)**

(ii) beam reduces to 25% in 2 half-lives **(1)**

$v (= 0.95 c) = 2.85 \times 10^8 \text{ m s}^{-1}$  **(1)**

distance =  $2 \times 27.5 \text{ ns} \times 2.85 \times 10^8 \text{ m s}^{-1}$  **(1)**  
=  $15.6 \text{ m}$  **(1)**

(6)

[9]