

**QUESTION one: WAVE MOTION**

The acceleration due to gravity =  $9.81 \text{ m s}^{-2}$

A cork floats on the surface of a pond across which a sinusoidal wave-train of wavelength 10 m and amplitude 0.20 m is travelling. The velocity,  $v$ , of waves of wavelength,  $\lambda$ , on a liquid surface is given by

$$v^2 = \frac{g\lambda}{2\pi} + \frac{2\pi\gamma}{\lambda\rho}$$

where  $\rho$  is the density ( $1.0 \times 10^3 \text{ kg m}^{-3}$  for water) and  $\gamma$  is the surface tension, which for water has the value  $7.2 \times 10^{-2} \text{ N m}^{-1}$ .

- (a) Show that the equation is dimensionally consistent.

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- (b) Calculate the wave speed.

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- (c) Calculate the maximum speed of the cork as it rises and falls in the water.

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Sea waves of wavelength 150 m and velocity of  $15.3 \text{ m s}^{-1}$  are heading North. A cruise ship is also travelling North at  $8.0 \text{ m s}^{-1}$ .

- (d) Calculate the frequency of the ship's up and down movement.

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- (e) The natural pitch period of the ship (the period of oscillation produced by pulling the front of a ship down in completely flat water) is about 8 s.

By considering the ship when it is travelling normal to the wavefront, explain why the ship must avoid certain speeds.

If the wave has a speed of  $10.8 \text{ m s}^{-1}$  and wavelength of 75 m, calculate the speeds that should be avoided.

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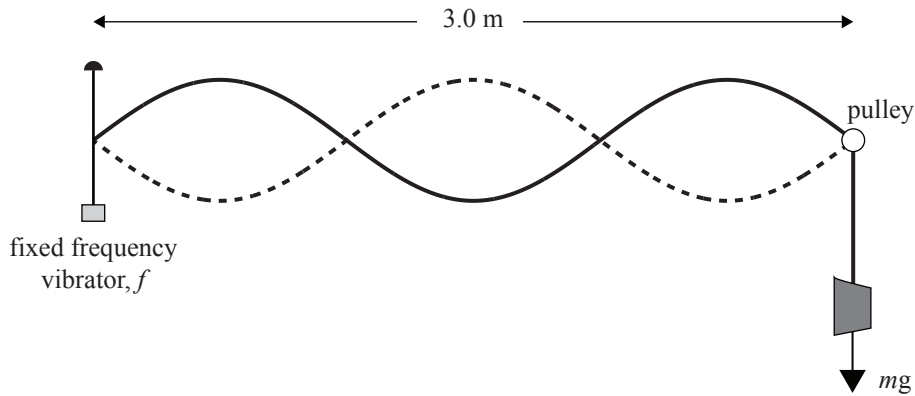
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## QUESTION TWO: ALL THINGS WAVES



A string, given a constant small amplitude by the vibrator of fixed frequency  $f$ , has the third harmonic standing wave established when under a tension of  $T = mg$ , as shown above.

- (a) Explain how a standing wave forms with this experimental arrangement.

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- (b) (i) The speed of a wave on a string is given by the relationship

$$v = \sqrt{\frac{T}{\mu}} \quad \text{where } \mu = \text{mass per unit length and } T \text{ is the tension.}$$

Show that the tension is given by the following expression:  $T = \mu f^2 \lambda^2$

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- (ii) Show that this expression for the tension is dimensionally correct.

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**QUESTION THREE: VIBRATING WIRES**

Acceleration due to gravity =  $9.81 \text{ m s}^{-2}$

Long wires, stretched between two points, can vibrate when a steady wind blows past them. Engineers, in dealing with the problems caused by these vibrations, have found it useful to define the Strouhal number,  $St$ , as  $St = f \frac{r}{v_w}$ , where  $f$  is the frequency of vibration,  $r$  is the radius of the wire, and  $v_w$  is the wind speed.

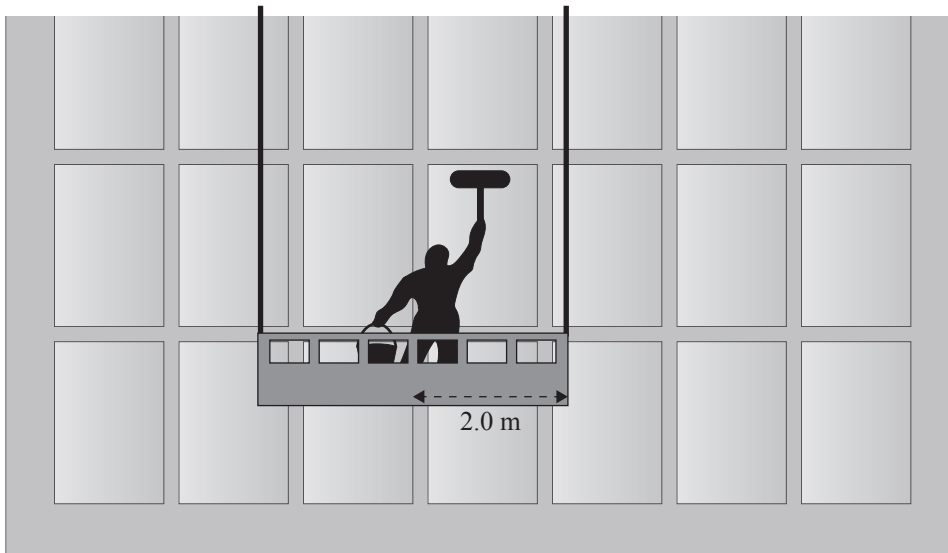
- (a) Show that the Strouhal number is dimensionless.

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A window-washing cradle of width  $4.0 \text{ m}$  is suspended from two cables of equal length.



A steady wind of  $10 \text{ m s}^{-1}$  causes the cables to vibrate with a frequency of  $200 \text{ Hz}$ . In this situation, a Strouhal number of  $0.20$  is typical. The wave speed in a wire is given as  $v = \sqrt{\frac{T}{\mu}}$ , where  $T$  is the tension and  $\mu$  is the mass/unit length.

- (b) Explain, using physical principles, why the wave speed in a wire depends on the tension and the mass/unit length.

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- (c) The cradle has a mass of 100 kg and the window washer, who is standing in the middle of the cradle, has a mass of 75 kg (including his mop and bucket).

Given that the density of the cable material is  $8.0 \times 10^3 \text{ kg m}^{-3}$ , show that the wave speed in the cables is  $18 \text{ m s}^{-1}$ .

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- (d) The window washer moves from the centre of the cradle to a position 1.0 m from the centre.

- (i) Compare the wavelengths of the vibrations in the two cables.

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- (ii) In this scenario, the window washer does not hear beats.

Explain the physical conditions required for him to hear beats from vibrations in the wires when he is standing in the window-washing cradle.

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**QUESTION FOUR: WAVES ON STRINGS**

The speed  $v$  of a wave on a string is given by,  $v = \sqrt{\frac{T}{\mu}}$ , where  $T$  is the tension in the string, and  $\mu$  is the mass per unit length, measured in  $\text{kg m}^{-1}$ .

- (a) Show that the above equation is dimensionally correct.

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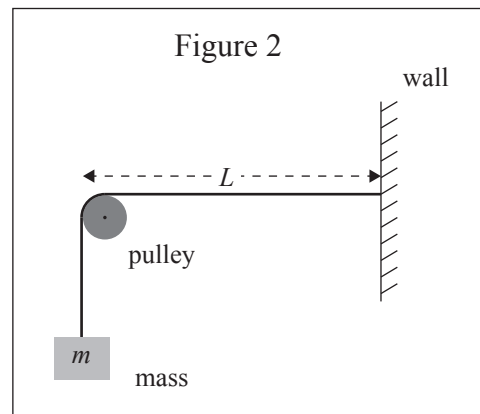
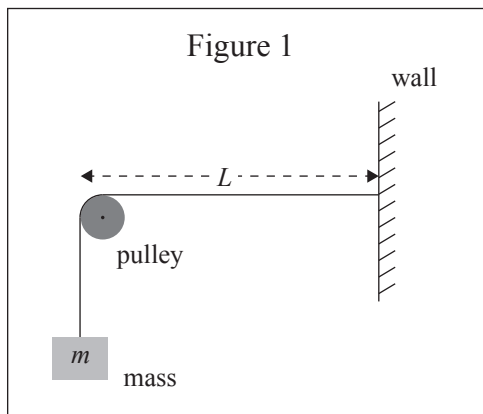
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- (b) One end of a string of mass per unit length  $\mu$  is attached to a solid wall, while the other end passes over a pulley, and is attached to a hanging mass,  $m$ , as shown in Figure 1.

A second string of the same length and made of the same material, but with twice the diameter, is mounted in a similar fashion with an identical mass,  $m$ , as shown in Figure 2.

The first string oscillates in its first harmonic when it is driven at a frequency of 200 Hz.

Calculate the frequency that will cause the second string to oscillate in its third harmonic.




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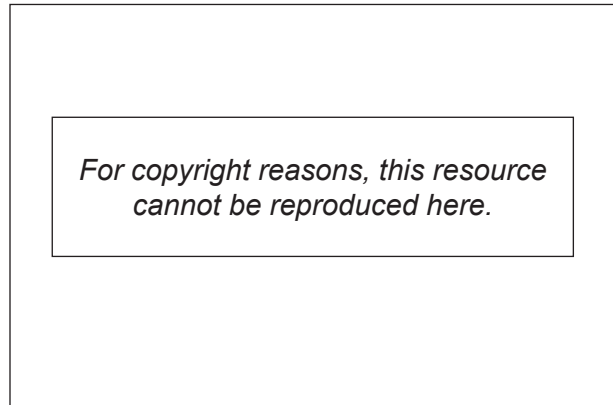


**QUESTION FIVE: CLARINETS AND FLUTES (8 marks)**



**Clarinet**

[www.life123.com/arts-culture/musical-instruments/clarinets/history-of-the-clarinet.shtml](http://www.life123.com/arts-culture/musical-instruments/clarinets/history-of-the-clarinet.shtml)



**Flute**

<http://miami.olx.com/flute-lessons-are-dynamic-excellent-results-iid-26298197>

The flute is played by blowing air over a large opening.

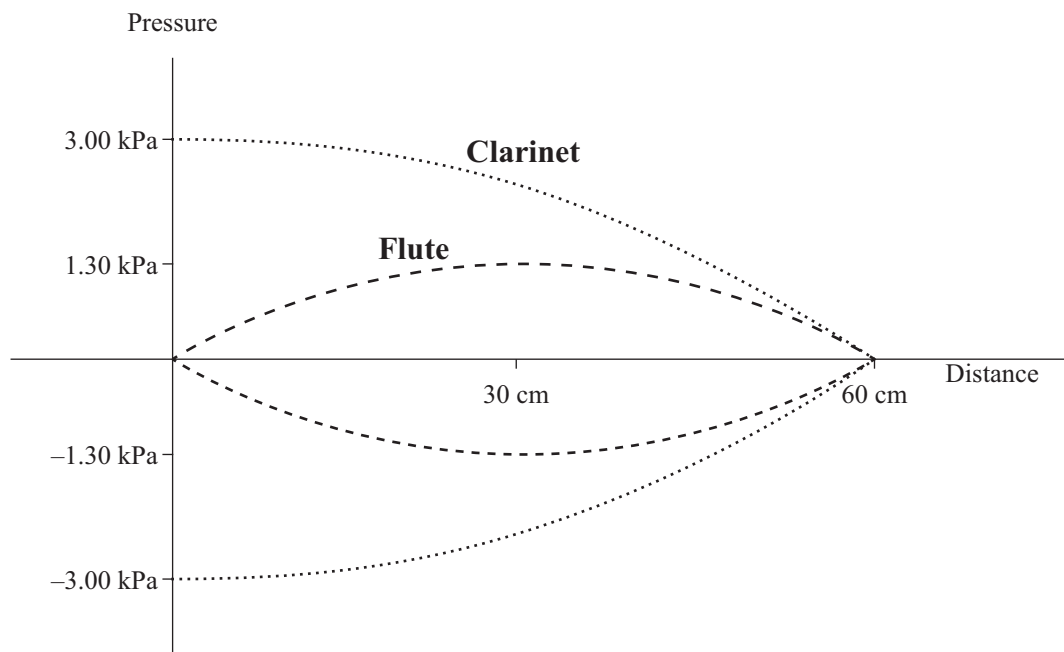


The clarinet is played by blowing air through a small opening covered by a vibrating reed.



The “acoustic pressure” in these wind instruments is the difference between the air pressure inside the instrument and the atmospheric pressure outside.

When the acoustic pressure is measured inside a flute and inside a clarinet, the maximum and minimum pressures are found to vary along the length of the instruments, as shown in the following graph. (Both the flute and the clarinet are 60 cm long, with the opening at 0 cm.)



- (a) Explain why, at each point inside the instruments, the pressure is recorded as having both a positive and a negative value.

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- (b) At the left hand end (where the reed is positioned) of the clarinet pipe, the acoustic pressure is a maximum.

Explain why there is a displacement node at this end of the clarinet.

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- (c) It is possible to blow some wind instruments harder so that the sound is **double** the frequency of the fundamental.

Explain why this is possible with a flute and is not possible with a clarinet.

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- (d) When the wind instrument is being played, the air inside can warm up and the notes played become sharper (have a slightly higher frequency).

Explain why this happens.

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- (e) Explain how standing sound waves can occur in open pipes.

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- (c) By analogy with a pipe with one open end, show that the period of the fundamental pulsation,  $T$ , of the variable star is given by,  $T = \frac{4R}{v_{av}}$ , where  $R$  is the equilibrium radius of the star, and  $v_{av}$  is the average speed of sound in the star.

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- (d) A typical white dwarf star is composed of material with a bulk modulus of  $1.33 \times 10^{22}$  Pa, density of  $1 \times 10^{10}$  kg m<sup>-3</sup> and a radius equal to  $9.0 \times 10^{-3}$  × solar radius. The bulk modulus is a measure of the compressibility of the material – a high bulk modulus indicates a high degree of incompressibility.

It can be shown that in a fluid or gas, the average speed of sound is given by the following relationship,  $v_{av} = \sqrt{\frac{\beta}{\rho}}$  where  $\beta$  = bulk modulus and  $\rho$  = density.

By using this relationship and that given in (c), calculate the pulsation period for a typical white dwarf star.

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