

Marking Scheme

#1

Question			Marking details	Marks Available
5	(a)		$\omega = \frac{2\pi(1200)}{60}$ (conversion of units (1)) = 125.7 [rad s ⁻¹] (1) $F = m\omega^2 r = (0.80)(125.7)^2(0.25)$ (subs (1)) = 3160.1 [N] (1)	4
	(b)	(i)	$R - mg = 3\,160.1$ (1) $R = 3\,160.1 + (0.8)(9.81) = 3\,168$ [N] (1) ecf from (a)	3
		(ii)	$R + mg = 3\,160.1$ $R = 3\,160.1 - (0.8)(9.81) = 3\,152$ [N] (1) ecf from (a)	
	(c)		Resonance – frequency of rotation matches the natural / resonant frequency of vibration of the saucepan [lid] (1) [When the spin rate decreases,] the frequencies no longer match / so no resonance (1)	2
			Question 5 Total	[9]

#2

Question			Marking details	Marks available				Maths	Prac
				AO1	AO2	AO3	Total		
1	(a)	(i)	Velocity [of car] is changing [with time] (1) because its direction is changing [so the car is accelerating] (1) or There is a <u>resultant</u> force (1) [towards the centre] due to friction / grip (1)	2			2		
		(ii)	$v = \frac{45 \times 10^3}{60 \times 60} = 12.5 \text{ m s}^{-1}$ (conversion) (1) $\omega = \frac{v}{r} = \frac{12.5}{80} = 0.156 \text{ rad s}^{-1}$ substitution and calculation (1)		2		2	2	
		(iii)	$a = \frac{v^2}{r} = \frac{(12.5)^2}{80}$ substitution (ecf) (1) [Alt: use $a = \omega^2 r$] = 1.95 m s ⁻² (1) Direction: towards centre (of 'circular' motion) (1)	1 1	1		3	2	
	(b)		Either: Any two × (1) of these points - Appropriate tyre design for friction - Banking of road [for contribution from normal contact force] - Appropriate surface - Suspension set-up - Anti-roll bars. (or any sensible answers, one referring to road and the other to the car) Or any one sensible point (1) + explanation of the role of physics (1) [			2	2		
			Question 1 total	4	3	2	9	4	0

Question				Marking details	Marks available					
					AO1	AO2	AO3	Total	Maths	Prac
	(a)	(i)		T tension in the string and mg weight of mass (gravitational force or gravity)	1			1		
		(ii)		T does not have a component tangential to the arc (1) Component of mg tangential to the arc is $mg \sin \theta$, (1) this is in the opposite direction to s (or θ) and so the negative sign (1)		3		3	1	
		(iii)		$\text{acceleration} = \frac{-mg \sin \theta}{m} = -g \sin \theta$ $= -g \theta \text{ (1) (using the approximation)}$ $\theta = \frac{s}{l} \text{ or } \sin \theta = \frac{s}{l} \text{ (1)} = -\frac{gs}{l}$		2		2	2	
		(iv)		Acceleration $\propto \theta$ (or s) measured [from a fixed position] (1) and opposite in direction (-ve) so SHM (1)			2	2		
	(b)	(i)	I	Substitution: $T = 2\pi \sqrt{\frac{l}{g}} = 2\pi \sqrt{\frac{1.2}{9.81}} \text{ (1)}$ $= 2.20 \text{ [s]} \text{ (1)}$	1	1		2	2	
			II	$f = \frac{1}{T} = 0.45 \text{ [5] [H]z}$ ecf (1)		1		1	1	
		(ii)		For maximum distance along the arc $\theta_{\max} = 0.067$, also $\sin \theta_{\max} = 0.067$ As $\theta_{\max} = \sin \theta_{\max}$ (i.e. for the largest value of θ) (1) then $\sin \theta$ is equal to θ for all θ , and approximation holds for SHM. System oscillates with SHM (1)			2	2	1	
				Question total	2	7	4	13	7	0

Question			Marking details	Marks available					
				AO1	AO2	AO3	Total	Maths	Prac
2	(a)		Angle when arc [length] equals radius Accept about 57.3° or angle when $2\pi = 360^\circ$ or cycle / circle	1			1		
	(b)	(i)	Use of $T = \frac{1}{f}$ (1) Answer = $1.67 \text{ [s]} \text{ (1)}$ Accept $\frac{5}{3}$ or 1.66 or $1.\dot{6}$ or 1.7 [s] Don't accept 1.6 [s]	1	1		2	1	
		(ii)	Substitution into $\omega = \frac{2\pi}{T}$ or $2\pi f$ or and $v = \omega r$ (1) ecf on T or f $v = 10.6 \text{ [m s}^{-1}\text{]} \text{ (1)}$ (Accept 10.5 m s^{-1} if 1.67 s used)		2		2	2	
	(c)		$N = \frac{mv^2}{r}$ or $mr\omega^2$ or implied (1) $N = \frac{66.2 \times (10.6)^2}{2.8} = [2\,634] \text{ [N]} \text{ (1)}$ ecf on v and ω accept approximately $2\,657 \text{ [N]}$ $F = 66.2 \times 9.81 = [649.4 \text{ [N]}] \text{ (1)}$ Vertical forces are balanced or equivalent e.g. $F = W$ (1)	1 1	1 1		4	2	
	(d)	(i)	$650 \leq \text{or} = \text{or} < \mu \times 2\,600 \text{ (1)}$ So $\mu > \text{or} = 0.24$ or 0.25 (1) Alternative: $2\,600 \times 0.25 \text{ (1)}$ $= 650 \text{ (1)}$	1	1		2	2	
		(ii)	Friction = 650 [N] or implied (1) $\frac{650}{0.45} = 1\,444 \text{ [N]} \text{ (1)}$ Equating to centripetal (1) $\omega = 2.8 \text{ [rad s}^{-1}\text{]} \text{ (1)}$ Answer of $2.51 \text{ [rad s}^{-1}\text{]}$ award 1 mark only		1	1 1 1	4	2	
			Question 2 total	5	7	3	15	9	0

(a)	(i)	$\omega = \frac{45(2\pi)}{60} = 4.71 \text{ [rad s}^{-1}\text{]}$ Conversion from rotations to radians, with the '45'. (1) Conversion from minutes to seconds and convincing working. (1)	2
	(ii)	$\text{velocity} = \omega r = (4.71)(0.08) = 0.38 \text{ [m s}^{-1}\text{]}$ Formula and substitution. (1) Result. (1)	2
	(iii)	$\text{acceleration} = \omega^2 r = (4.71)^2 (0.08) = 1.77 \text{ [m s}^{-2}\text{]}$ Formula and substitution. (1) Result (1)	2
	(iv)	Towards point Q, or towards centre of circle.	1
(b)	(i)	$A = 0.080 \text{ [m]}$	1
	(ii)	$T = \frac{2\pi}{\omega} = \frac{2\pi}{4.71} = 1.33 \text{ [s]}$	1
	(iii)	$a = -1.77 \sin(4.71 \times 0.20) = -1.43 \text{ [m s}^{-2}\text{]}$ Substitution of time (1). Result with minus sign (1)	2
	(iv)	A body moves with SHM if its acceleration - is directly proportional to its displacement from a fixed point - is always directed towards that [fixed] point 1 for: each statement	2
	(v)	$a = -\omega^2 A \sin(\omega t);$ $x = A \sin \omega t$ so substitution gives: $a = -\omega^2 x$ convincing manipulation. (1) final expression linking to SHM.(1)	2
(c)		$x = 0.06 \sin\left(4.71t - \frac{\pi}{2}\right).$ 1 for: each correct parameter inserted.	3

Question		Marking details	Marks available																																			
			AO1	AO2	AO3	Total	Maths	Prac																														
	(a)	Distance moved by mass P in 1 period, T (i.e. in one rotation) = $2\pi R$ and speed = distance / time = $\frac{2\pi R}{T}$ Alternative: $\omega = \frac{2\pi}{T}$ and $v = \omega R$		1		1	1	1																														
	(b)	<table border="1"><thead><tr><th>R / m</th><th>Time of 10 rot / s</th><th>T / s</th><th>v / m s⁻¹</th><th>v^2 / m² s⁻²</th></tr></thead><tbody><tr><td>0.50</td><td>4.7</td><td>0.47</td><td>6.68</td><td>44.6</td></tr><tr><td>0.60</td><td>5.2</td><td>0.52</td><td>7.25</td><td>52.6</td></tr><tr><td>0.70</td><td>5.6</td><td>0.56</td><td>7.85</td><td>61.6</td></tr><tr><td>0.80</td><td>6.0</td><td>0.60</td><td>8.38</td><td>70.2</td></tr><tr><td>0.90</td><td>6.3</td><td>0.63</td><td>8.98</td><td>80.6</td></tr></tbody></table> T column: All values correct (1) For column v all values correct (1) For column v^2 all values correct ecf (1) Consistent use of sig figs in each column and 2 or 3 sig figs (1)	R / m	Time of 10 rot / s	T / s	v / m s ⁻¹	v^2 / m ² s ⁻²	0.50	4.7	0.47	6.68	44.6	0.60	5.2	0.52	7.25	52.6	0.70	5.6	0.56	7.85	61.6	0.80	6.0	0.60	8.38	70.2	0.90	6.3	0.63	8.98	80.6		4		4	4	4
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	(c) (i)	Centripetal force = $0.010 \frac{v^2}{R}$ (1 for $\frac{mv^2}{R}$; 1 if value inserted for m)	1	1		2	1	2																														
	(ii)	Forces acting on mass Q: $0.090g - \tau = 0$ τ : tension (1) So $\tau = 0.090g$. Substitution for τ into (c)(i) (1) $0.090g = 0.010 \frac{v^2}{R}$ $v^2 = \frac{0.090g}{0.010} R$ $v^2 = 9g R$ clear and convincing working (1)		3		3	2	3																														
	(d) (i)	Axes, suitable choice scales (no multiples of 3) and labels on both axes (1) – scales to occupy more than half of paper All points plotted correctly to $\pm \frac{1}{2}$ small square division (2) 4 points plotted correctly to $\pm \frac{1}{2}$ small square division award 1 mark 1-3 points plotted correctly to $\pm \frac{1}{2}$ small square division award 0 marks Line of best fit (1)		4		4	4	4																														
	(ii)	gradient = $\frac{50.0}{0.56} = 89.286 \text{ m s}^{-2}$; find gradient from best fit line (1) also gradient = $9g$ general method (1) $9g = 89.286$ $g = \frac{1}{9} \times 89.286 = 9.92 \text{ m s}^{-2}$ unit mark (1)																																				

			$g = \frac{89.286}{9} = 9.92 \text{ m/s}^2$ unit mark (1) (Accept $g = 8.8$ to 10.8 m/s^2 i.e. uncertainty of ~10%.) Use of single data point award a maximum of 2 marks			3	3	3	3
		(iii)	Take measurements for each value of R several times or measure time of more rotations or use of video capture or increase radius and period Accept repeat readings Don't accept have an assistant			1	1		1
			Question total	1	13	4	18	15	18

#7

(a)	[centripetal force =] $m\omega^2 r$ [or $\omega^2 r$ and ma] (1) $F = 32.5 \times 1.4^2 r$ [= 63.7 r] (1) Friction [of the surface on the shoes] provides centripetal force [or is the resultant etc.] (1) [Accept $F = m\omega r^2$ for 1st and 3rd marks as F is defined in the question]	3
(b)	63.7 $r = 114$ [N] (1) $r = 1.79$ and relevant comment, e.g. if r greater, $F > 114$ N (1) [Alt: Subst $r = 1.8$ m and comment that $F > 114$ N]	2
(c)	$T = \frac{2\pi}{\omega}$ [or by impl.] (1) [= $\frac{2\pi}{1.4}$] 4.49 s (1)	2
(d)	$v = \omega A$ [or by impl.] (1) [= 1.4×1.8] 2.52 m s⁻¹ (1) [If $v = A\omega \cos \omega t$, or equiv, then $\cos \omega t = 1$ must be stated for 1st mark]	2
(e)	$a = \omega^2 A$ [or by impl.] (1) [= $1.4^2 \times 1.8$] 3.53 m s⁻² (1) occurs at the extremities / when $x = \pm A$ etc. (1) [If $a = A\omega^2 \cos \omega t$, or equiv, then $\cos \omega t = 1$ must be stated for 1st mark]	3
(f)	At least one cycle of wave drawn with correct amplitude [1.8 m e.c.f.] (1) Reasonable shape of sinusoid + correct period + correct phase [i.e. sin wave] (1)	2
(g)	Use of $-1.00 = \sin \omega t$ (1) $1.4t = \sin^{-1}\left(\frac{-1}{1.8}\right)$ (1) [= -0.59] $t = -0.42$ s (1) [Mysterious loss of - sign loses 1 mark] $t_1 = \frac{T}{2} + 0.42$ [2.42 s] and $t_2 = T - 0.42$ [4.07 s] (1) Max 2 marks for reading from graph ± 0.1 s, i.e. 2.6, 2.7 s ✓ 4.0, 4.1 s ✓	4
		[18]

Question			Marking details	Marks available				Maths	Prac
				AO1	AO2	AO3	Total		
	(a)	(i)	Use of the equation $\frac{M_2 d}{(M_1 + M_2)} = x$ even if wrong M_2 (1) $\frac{9.2 \times 10^{24} \times 5.3 \times 10^{10}}{(9.5 \times 10^{24} + 9.2 \times 10^{24})}$ seen (1) ({ $+9.2 \times 10^{24}$ } can be omitted from the above equation) or 513 263 [m] seen etc.	1 1			2	2	
		(ii)	$v = \frac{2\pi r}{T}$ applied or $v = \omega r$ and $\omega = \frac{2\pi}{T}$ combined (1) Conversion of 130 days ($130 \times 24 \times 3600$) (1) Answer = 0.287 [m s ⁻¹] (ecf on day conversion) (1)	1	1 1		3	3	
		(iii)	Redshift is small or the redshift is proportional to velocity or small $\Delta\lambda$ or shown using the Doppler equation (1) Small wavelength change is difficult to measure or shifted wavelength is too close to the original (1)		2		2		
	(b)	(i)	$F = \frac{GMm}{r^2}$ used (1) Answer = 2.08×10^{23} [N] (1)	1	1		2	2	
		(ii)	Method for obtaining stress i.e. $\frac{F}{A}$ (1) 1.35×10^9 [Pa] (1) Correct conclusion e.g. the steel bar would break ecf (1) Theory doesn't work / Newton's grav law used successfully for centuries / won't work for elliptical orbits / would melt (1) Alternative: Use of $F = \alpha A$ (1) $F = 6.9 \times 10^{22}$ [N] (1)			4	4	2	
	(c)	(i)	$\text{PE} = -\frac{GMm}{r}$ used N.B. ecf if $\text{PE} = Fr$ used (1) Answer = [-] 1.10×10^{34} [J] (1)	1	1		2	2	
		(ii)	Realising KE is involved (1) Correct variation with distance for KE or velocity or as PE increases KE decreases or converse (1)			2	2		
			Question total	5	6	6	17	11	0

